

# Prerequisite Relation Learning for Concepts in MOOCs

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# **Outline**



## **Backgrounds**

**Problem Definition** 

Methods

**Experiments and Analysis** 

**Conclusion** 







What? Prerequisite Relation Learning for Concepts in MOOCs







# **Prerequisite Relation Learning for Concepts in MOOCs**

• Massive open online courses (MOOCs) have become increasingly popular and offered students around the world the opportunity to take online courses from prestigious universities.













## **Prerequisite Relation Learning for Concepts in MOOCs**

 Massive open online courses (MOOCs) have become increasingly popular and offered students around the world the opportunity to take online courses from prestigious universities.













## **Prerequisite Relation** Learning for Concepts in MOOCs

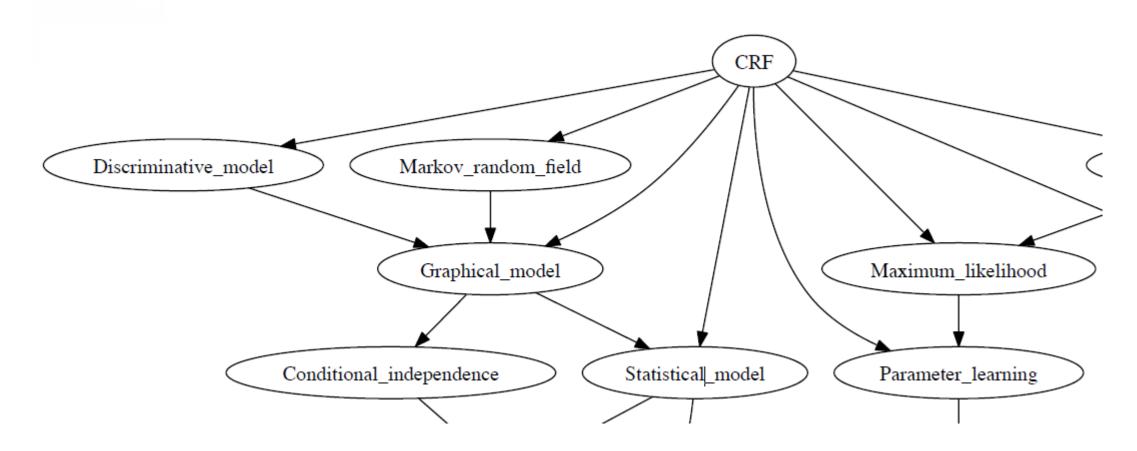
- A *prerequisite* is usually a concept or requirement before one can proceed to a following one.
- The prerequisite relation exists as a natural dependency among concepts in cognitive processes when people learn, organize, apply, and generate knowledge (Laurence and Margolis, 1999).







# **Prerequisite Relation** Learning for Concepts in MOOCs



Partha Pratim Talukdar and William W Cohen. Crowdsourced comprehension: predicting prerequisite





## **Prerequisite Relation Learning for Concepts in MOOCs**

### **Motivation 1**. Manually building a concept map in MOOCs is infeasible

• In the era of MOOCs, it is becoming infeasible to manually organize the knowledge structures with thousands of online courses from different providers.

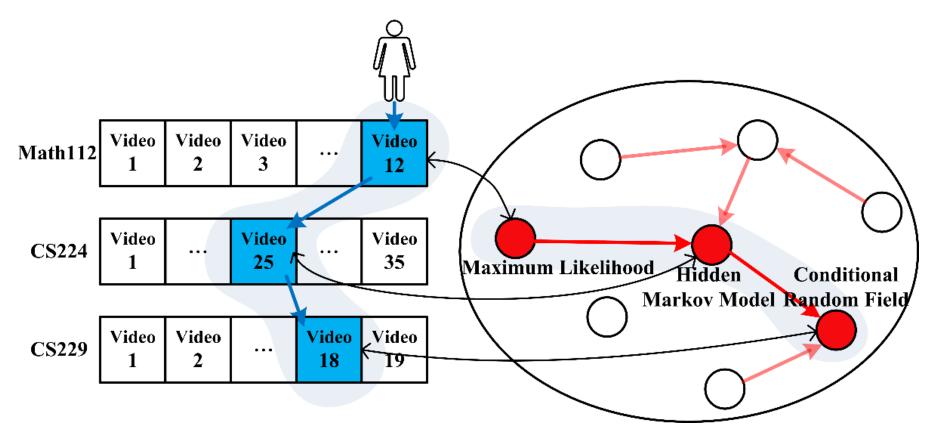
### **Motivation 2**. To help improve the learning experience of students

• The students from different background can easily explore the knowledge space and better design their personalized learning schedule.





Question: What should she get started if she wants to learn the concept of "conditional random field"?



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## Problem Definition



#### □ Input

■ MOOC Corpus  $\mathcal{D} = \{\mathcal{C}_1, \cdots, \mathcal{C}_i, \cdots, \mathcal{C}_n\}$ , where  $\mathcal{C}_i$  is one course

**Course** 
$$\mathcal{C} = (\mathcal{V}_1, \cdots, \mathcal{V}_i, \cdots, \mathcal{V}_{|\mathcal{C}|})$$
 , where  $v_i$  is the i-th **video** of course  $\mathcal{C}$ 

**Video** 
$$\mathcal{V} = (s_1 \cdots s_i \cdots s_{|\mathcal{V}|})$$
 , where  $s_i$  is the i-th **sentence** of video  $v$ 

**Course Concepts**  $\mathcal{K} = \mathcal{K}_1 \cup \cdots \cup \mathcal{K}_n$  , where  $K_i$  is the set of course concepts in  $C_i$ 

#### Output

Prerequisite Function

$$PF(a,b) \in \{0,1\}, \ a,b \in \mathcal{K}$$

The function *PF* predicts whether concept *a* is a prerequisite concept of *b* 



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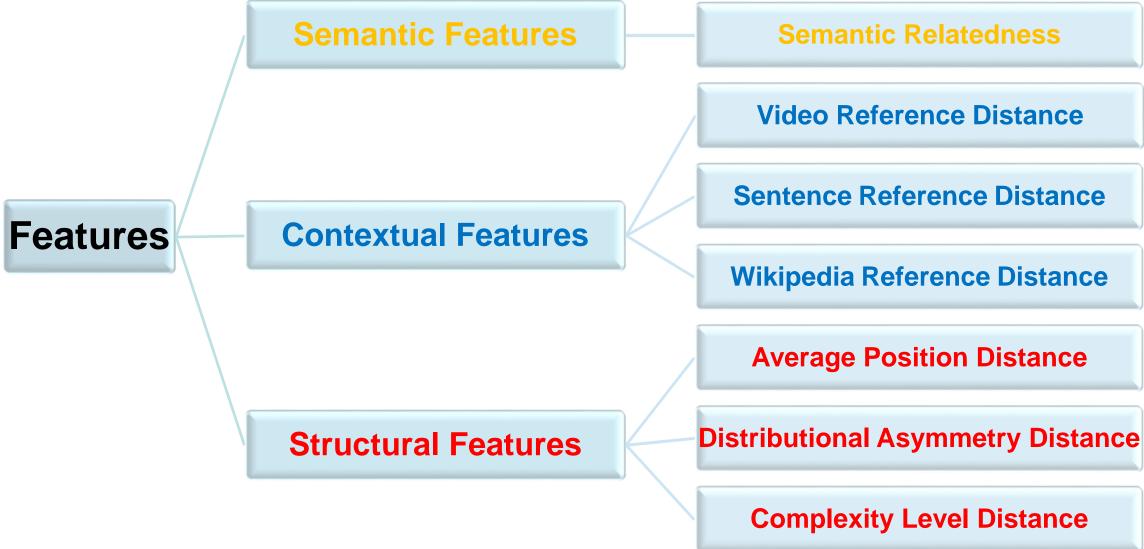
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## Features Overview





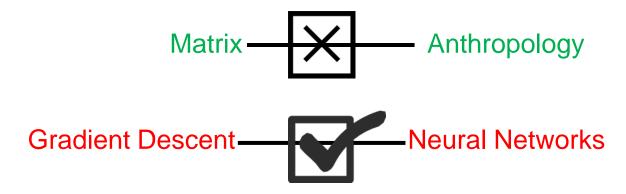


## Semantic Features



Features Semantic Features Semantic Relatedness

- Semantic Relatedness plays an important role in prerequisite relations between concepts.
- If two concepts have *very different semantic meanings*, it is *unlikely* that they have prerequisite relations.





## Semantic Features



#### Concept Embeddings

Wikipedia corpus

$$OE = \langle w_1 \cdots w_i \cdots w_m \rangle$$

- Procedure of Concept Embeddings
  - 1. Entity Annotation: We label all the entities in the Wikipedia corpus based on the hyperlinks in Wiki, and get a new corpus OE' and a wiki entity set ES.

$$OE' = \langle x_1 \cdots x_i \cdots x_{m'} \rangle$$
 $ES = \{ e_1 \cdots e_i \cdots e_w \}$ 

Where  $x_i$  corresponds to a word  $w \in OE$  or an entity  $e \in ES$ 

- 2. Word Embeddings: We apply the skip-gram model to train word embeddings on OE'.
- 3. Concept Representation: After training, we can obtain the vector for each concept in *ES*. For any non-wiki concept, we obtain its vector via the vector addition of its individual word vectors.



## **Features**

**Contextual Features** 

**Video Reference Distance** 

• If in videos where concept A is frequently talked about, the teacher also needs to refer to concept B for a lot but not vice versa, then B would more likely be a prerequisite of A.

#### **Back Propagation**



#### **Gradient Descent**







#### ■ Video Reference Distance

Video Set of the MOOC corpus

$$V^D = V_1 \cup \cdots V_n$$

■ Video Reference Weight from A to B

$$Vrw(A,B) = rac{\displaystyle\sum_{v \in V^D} f\left(A,v
ight) \cdot r(v,B)}{\displaystyle\sum_{v \in V^D} f\left(A,v
ight)}$$

Where

- f(A, v): the term frequency of concept A in video v
- $r(v, B) \in \{0,1\}$ : whether concept B appears in video v
- It indicates how B is referred by A's videos
- Video Reference Distance of (A,B)

$$Vrd(A,B) = Vrw(B,A) - Vrw(A,B)$$





#### □ Generalized Video Reference Distance

■ Generalized Video Reference Weight from A to B

Reference Weight from A to B
$$\sum_{i=1}^{K} Vrw(a_i,B) \cdot w(a_i,A) = rac{\displaystyle\sum_{i=1}^{K} Vrw(a_i,B) \cdot w(a_i,A)}{\displaystyle\sum_{i=1}^{K} w\left(a_i,A
ight)}$$

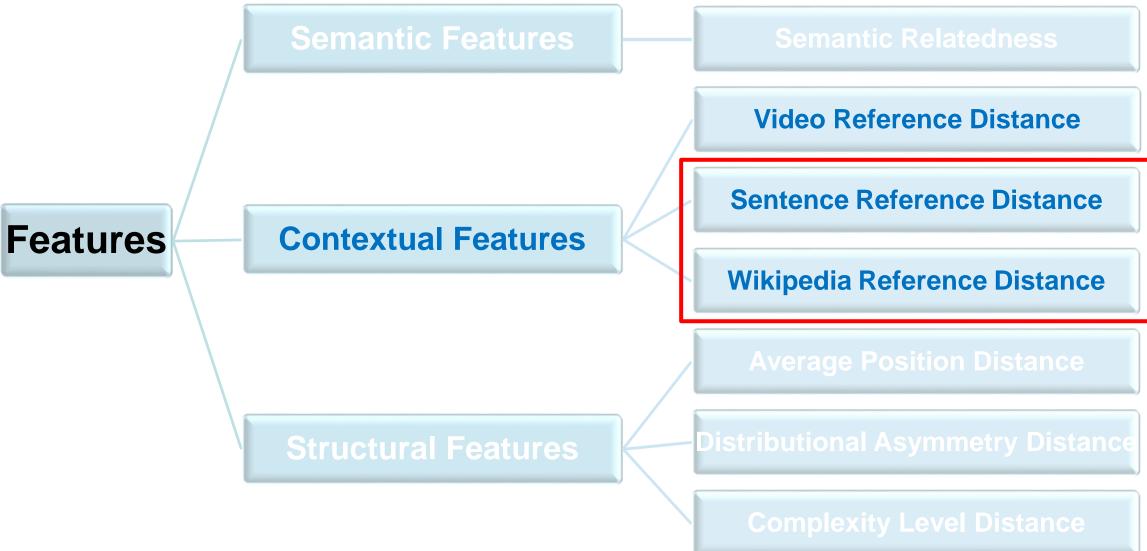
#### Where

- $\{a_1, \dots, a_K\}$ : the top-K most similar concepts of A, where  $a_1, \dots, a_K \in T$
- $w(a_i, A)$ : the similarity between  $a_i$  and A
- It indicates how B is referred by A's related concepts in their videos
- Generalized Video Reference Distance of (A,B)

$$GVrd(A,B) = GVrw(B,A) - GVrw(A,B)$$









Features

Structural Features

Complexity Level Distance

Distributional Asymmetry Distance

- In teaching videos, knowledge concepts are usually introduced based on their learning dependencies, so the structure of MOOC courses also significantly contribute to prerequisite relation inference in MOOCs.
- We investigate 3 different structural information, including *appearing positions of concepts*, *learning dependencies of videos* and *complexity levels of concepts*.





#### ■ Average Position Distance

- Assumption
  - In a course, for a specific concept, its prerequisite concepts tend to be introduced before this concept and its subsequent concepts tend to be introduced after this concept.
- $\blacksquare$  TOC Distance of (A,B)

$$Apd(A,B) = \begin{cases} \frac{1}{|C(A,B)|} \sum_{C \in C(A,B)} (AP(A,C) - AP(B,C)) , C(A,B) \neq \emptyset \\ 0 , C(A,B) = \emptyset \end{cases}$$

Where

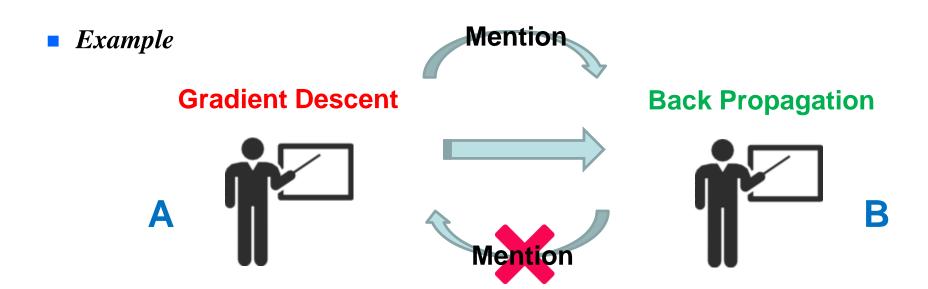
- C(A, B): the set of courses in which A and B both appear
- AP(A,C) = the average index of videos containing concept A in course C (*The average position of a concept A in course C*)





#### ■ Distributional Asymmetry Distance

- Assumption
  - The learning dependency of course videos is also helpful to infer learning dependency of course concepts.
  - Specifically, if video  $V_a$  is a precursor video of  $V_b$ , and a is a prerequisite concept of b, then it is likely that  $f(b, V_a) < f(a, V_b)$







- Distributional Asymmetry Distance
  - All possible video pairs of  $\langle a,b \rangle$  that have sequential relation

$$\mathcal{S}(\mathcal{C}) = \{(i,j)|i \in \mathcal{I}(\mathcal{C},a), j \in \mathcal{I}(\mathcal{C},b), i < j\}$$

■ Distributional Asymmetry Distance

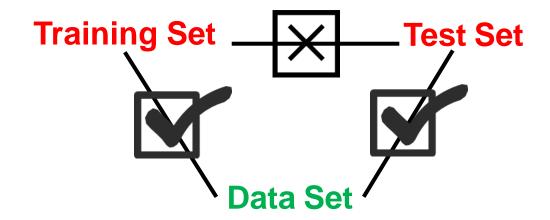
$$Dad\left(a,b
ight) = rac{\displaystyle\sum_{\left(i,j
ight) \in \mathcal{S}\left(\mathcal{C}
ight)} f\left(a,\mathcal{V}_{i}^{\,\mathcal{C}}
ight) - f(b,\mathcal{V}_{j}^{\,\mathcal{C}}
ight)}{\left|\mathcal{S}\left(\mathcal{C}
ight)
ight|}}{\left|\mathcal{C}\left(a
ight) \cap \mathcal{C}(b)
ight|}$$



#### Complexity Level Distance

- Assumption
  - If two related concepts have prerequisite relationship, they may have a difference in their complexity level. It means that one concept is more *basic* while another one is more *advanced*.

#### Example







#### Complexity Level Distance

- Assumption
  - For a specific concept, if it **covers more videos** in the course or it **survives longer time** in a course, then it is more likely to be a general concept rather than a specific concept.
- Average video coverage of A

$$AVC(A) = rac{1}{C(A)} \sum_{C \in C(A)} rac{vc(A)}{m_C}$$

Average survival time of A

$$AST(A) = \frac{1}{C(A)} \sum_{C \in C(A)} \frac{LI(A) - FI(A) + 1}{m_C}$$

■ Complexity Level Distance of (A,B)

$$Cld(A,B) = AVC(A) \cdot AST(A) - AVC(B) \cdot AST(B)$$



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# Experimental Datasets



# Collecting Course Videos

 "Machine Learning" (ML), "Data Structure and Algorithms" (DSA), and "Calculus" (CAL) from Coursera

#### Course Concepts Annotation

 Extract candidate concepts from documents of video subtitles Label the candidates as "course concept" or "not course concept"

# Prerequisite Relation Annotation

 We manually annotate the prerequisite relations among the labeled course concepts.



# Experimental Datasets



#### □ Dataset Statistics

■ 3 novel datasets extracted from Coursera

• ML: 5 Machine Learning courses

• DSA: 8 Data Structure and Algorithms courses

• CAL: 7 Calculus courses

Dataset	#courses #videos #concepts			#pai	$\kappa$	
				_	+	
ML	5	548	244	5,676	1,735	0.63
DSA	8	449	201	3,877	1,148	0.65
CAL	7	359	128	1,411	621	0.59

## **Evaluation Results**



#### □ Models

- Naïve Bayes (NB)
- Logistic Regression (LR)
- SVM with linear kernel (SVM)
- Random Forest (RF)

#### □ Metrics

- Precision (P)
- Recall (R)
- F1-Score (F1)
- □ 5-Fold Cross Validation

Classifier		ML		DSA		CAL	
	M	1	10	1	10	1	10
	P	63.2	60.1	60.7	62.3	61.1	61.9
SVM	R	68.5	72.4	69.3	67.5	<b>67.9</b>	68.3
	$F_1$	65.8	65.7	64.7	64.8	64.3	64.9
	P	58.0	58.2	62.9	62.6	60.1	60.6
NB	R	58.1	60.5	62.3	61.8	61.2	62.1
	$F_1$	58.1	59.4	62.6	62.2	60.6	61.3
	P	66.8	67.6	63.1	62.0	62.7	63.3
LR	R	60.8	61.0	64.8	66.8	63.6	64.1
	$F_1$	63.7	64.2	63.9	64.3	61.6	62.9
	P	68.1	71.4	69.1	72.7	67.3	70.3
RF	R	70.0	<b>73.8</b>	68.4	72.3	67.8	71.9
	$F_1$	69.1	<b>72.6</b>	<b>68.7</b>	72.5	67.5	71.1

Table 2: Classification results of the proposed method(%).



# Comparison with Baselines



#### Comparison Methods

#### Hyponym Pattern Method (HPM)

• This method simply treat the concept pairs with IS-A relations as prerequisite concept pairs.

#### Reference Distance (RD)

• This method was proposed by Liang et al. (2015). However, this method is only applicable to Wikipedia concepts.

#### Supervised Relationship Identification (SRI)

- Wang et al. (2016) has employed several features to infer prerequisite relations of Wikipedia concepts in textbooks, including 3 Textbook features and 6 Wikipedia features.
- (1) **T-SRI:** only textbook features are used to train the classifier.
- (2) **F-SRI:** the original version, all features are used.



# Comparison with Baselines



- W-ML, W-DSA, W-CAL are subsets with Wikipedia Concepts
- □ HPM achieves relatively high precision but low recall.
- T-SRI only considers relatively simple features
- Incorporating Wikipedia-based features achieves certain promotion in performance

Method		ML	DSA	CAL	W- ML	W- DSA	W- CAL
НРМ	P	67.3	71.4	69.5	79.9	72.3	73.5
	R	18.4	14.8	16.5	25.5	27.3	23.3
	$F_1$	29.0	24.5	26.7	38.6	39.6	35.4
RD	P	_	_	_	73.4	77.8	74.4
	R	_	_	_	42.8	44.8	43.1
	$F_1$	_	_	_	54.1	56.8	54.6
T-SRI	P	61.4	62.3	62.5	58.1	60.1	62.7
	R	62.9	64.6	65.5	67.6	65.3	67.9
	$F_1$	62.1	63.4	64.0	62.5	62.6	65.2
F-SRI	P	_	_	_	64.3	64.3	64.8
	R	_	_	_	62.1	65.6	65.2
	$F_1$	_	_	_	63.2	64.9	65.0
	P	71.4	72.7	70.3	72.8	68.4	71.4
MOOC	CR	73.8	72.3	71.9	71.3	72.0	70.8
	$F_1$	72.6	72.5	71.1	72.0	70.2	71.1

Table 3: Comparison with baselines(%).



# Comparison with Baselines



#### □ Setting

- Each time, one feature or one group of features is removed
- We record the decrease of F1-score for each setting

#### Conclusion

- All the proposed features are useful
- Complexity Level Distance is most important
- **Semantic Relatedness** is least important

_		Ignored Feature(s)	P	R	$F_1$
_		Sr	69.6	72.9	71.2( <b>-1.4</b> )
		GVrd	68.8	71.4	70.1(-2.5)
		GSrd	67.9	71.4	69.6(-3.0)
	Single	Wrd	70.1	72.1	71.1(-1.5)
		Apd	69.7	70.8	70.2(-2.4)
		Dad	69.2	69.5	69.4(-3.2)
		Cld	64.9	65.6	65.2( <b>-7.4</b> )
t	Group	Semantic	69.6	72.9	71.2( <b>-1.4</b> )
		Contextual	66.4	68.9	67.6(-5.0)
		Structural	63.7	64.2	63.4( <b>-9.2</b> )

Table 4: Contribution analysis of different features(%).



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# Thanks!

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